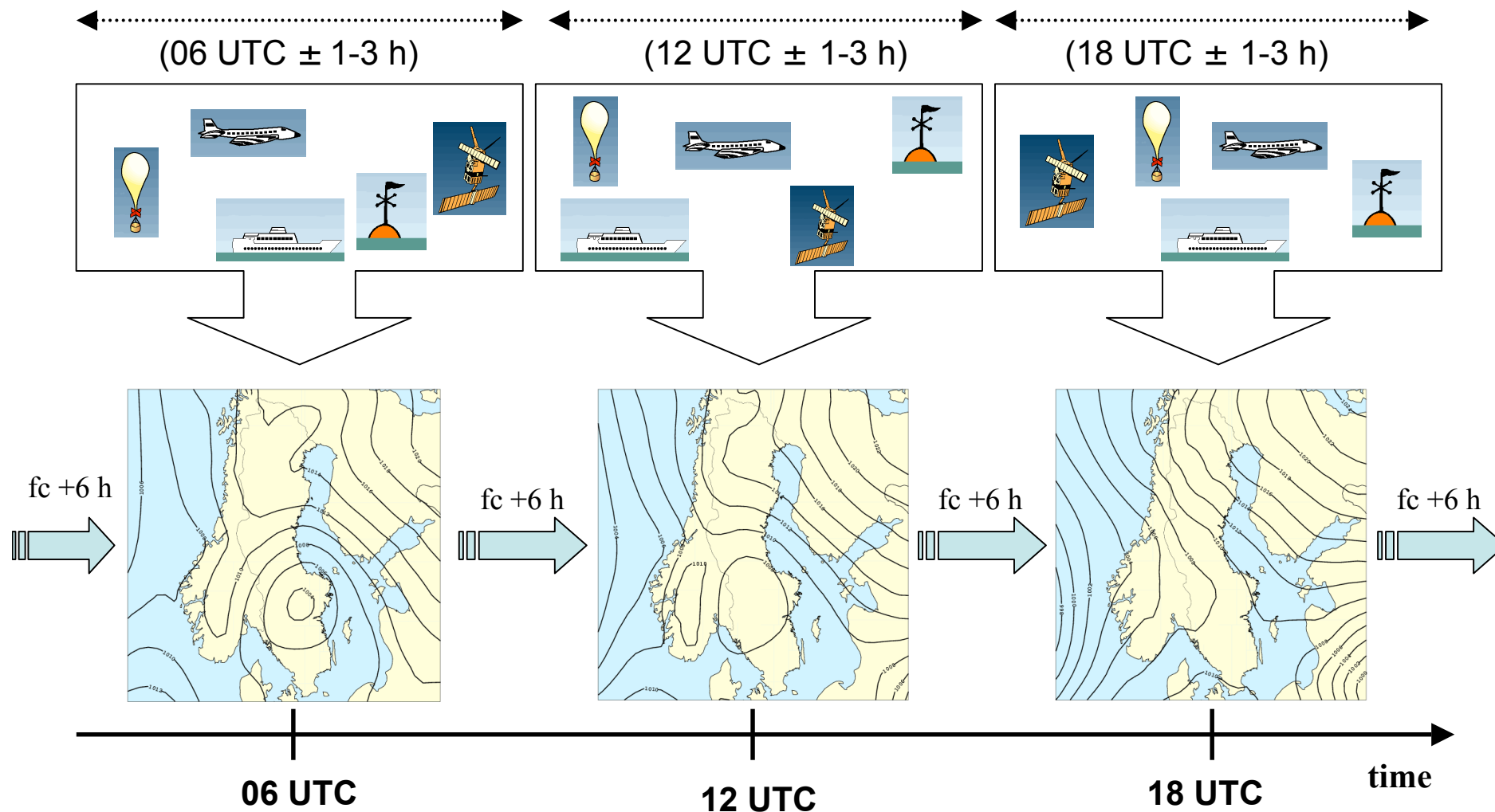


# Assimilation of ZTD data – error modelling

*Martin Ridal*

Swedish Meteorological and Hydrological Institute

# Intermittent data assimilation



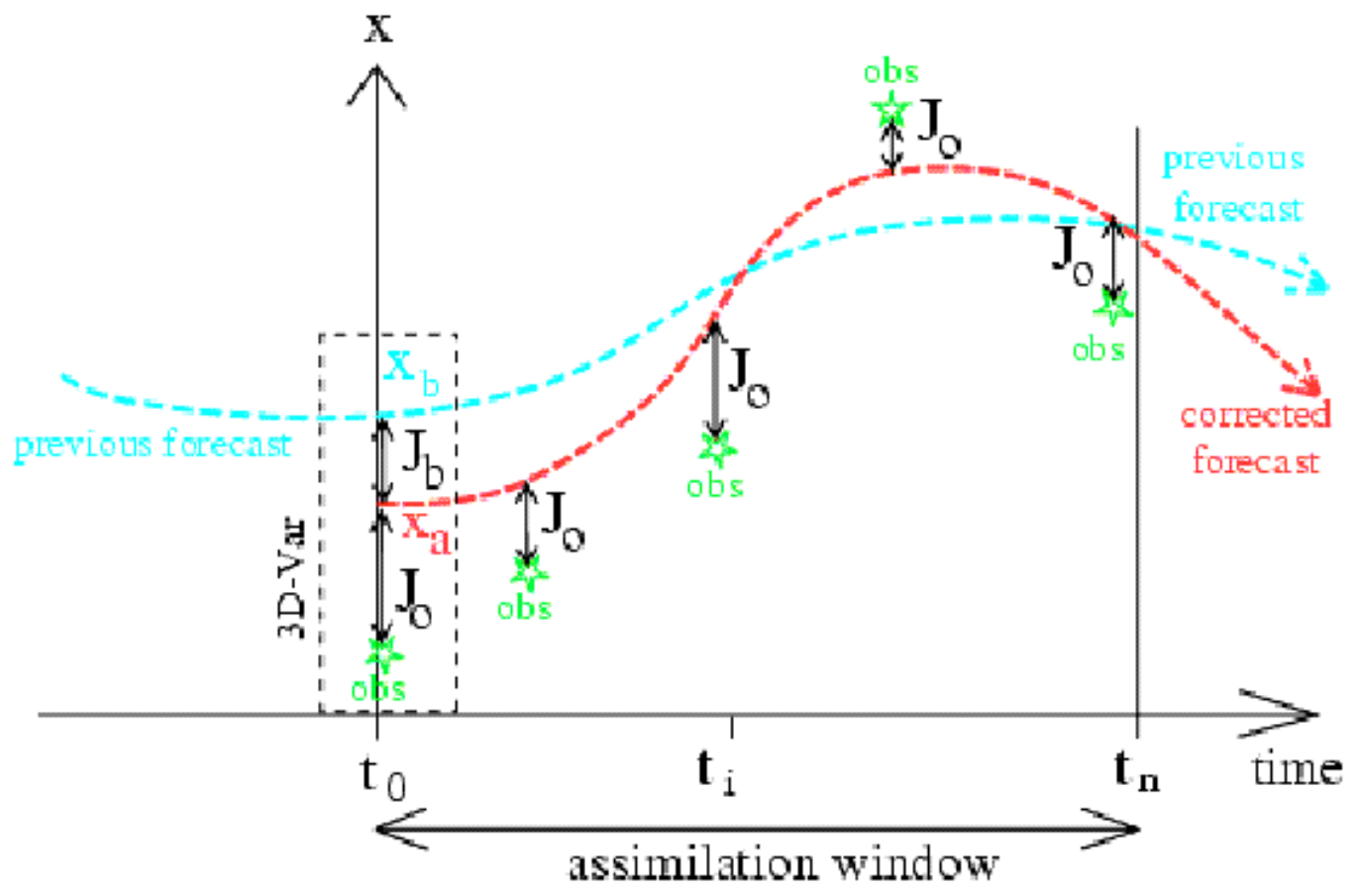
## 3- and 4-D variational assimilation

$J_b$  measures the distance between the analysis and a background field

$J_o$  measures the distance between the analysis and the observations

The minimum of  $J_b + J_o$  is our analysis

$$J = J_b + J_o = \frac{1}{2} (\mathbf{x} - \mathbf{x}_b)^T \mathbf{B}^{-1} (\mathbf{x} - \mathbf{x}_b) + \frac{1}{2} (H\mathbf{x} - \mathbf{y})^T \mathbf{R}^{-1} (H\mathbf{x} - \mathbf{y})$$



## *The moisture problem*

### Difficult quantity

- Large variations
- Small scale

### Until now very few observations

- Radiosondes
- Very sparse coverage both spatially and temporally

### Poor initialisation

- 2- or 3-D interpolation
- No feedback to pressure or wind fields

### Many tuning parameters in the model

- The model is not ready for the new amounts of data
- New moisture information is wiped out by the dynamics

## *Solutions to the moisture problem*

### Better initialisation

- ...with feedback to (and from) other model variables

### A new control variable for moisture

- Normalised relative humidity
- Gaussian error structure (but not at extremes)
- Results in removal of tuning parameters

### 4D-Var

- Better constructed from the start

### Understanding the measurements

- Often complicated error characteristics
- Non-linear processes and errors
- Small scale

# GPS moisture assimilation

*“One person’s noise is another person’s signal”*

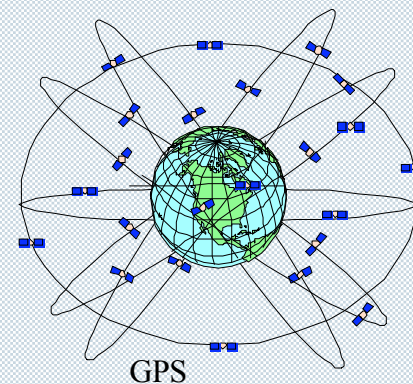
## Ground based GPS

### Advantages:

- High resolution
- 55 to 60 stations every 15 minutes
- All weather, all the time
- Very cheap

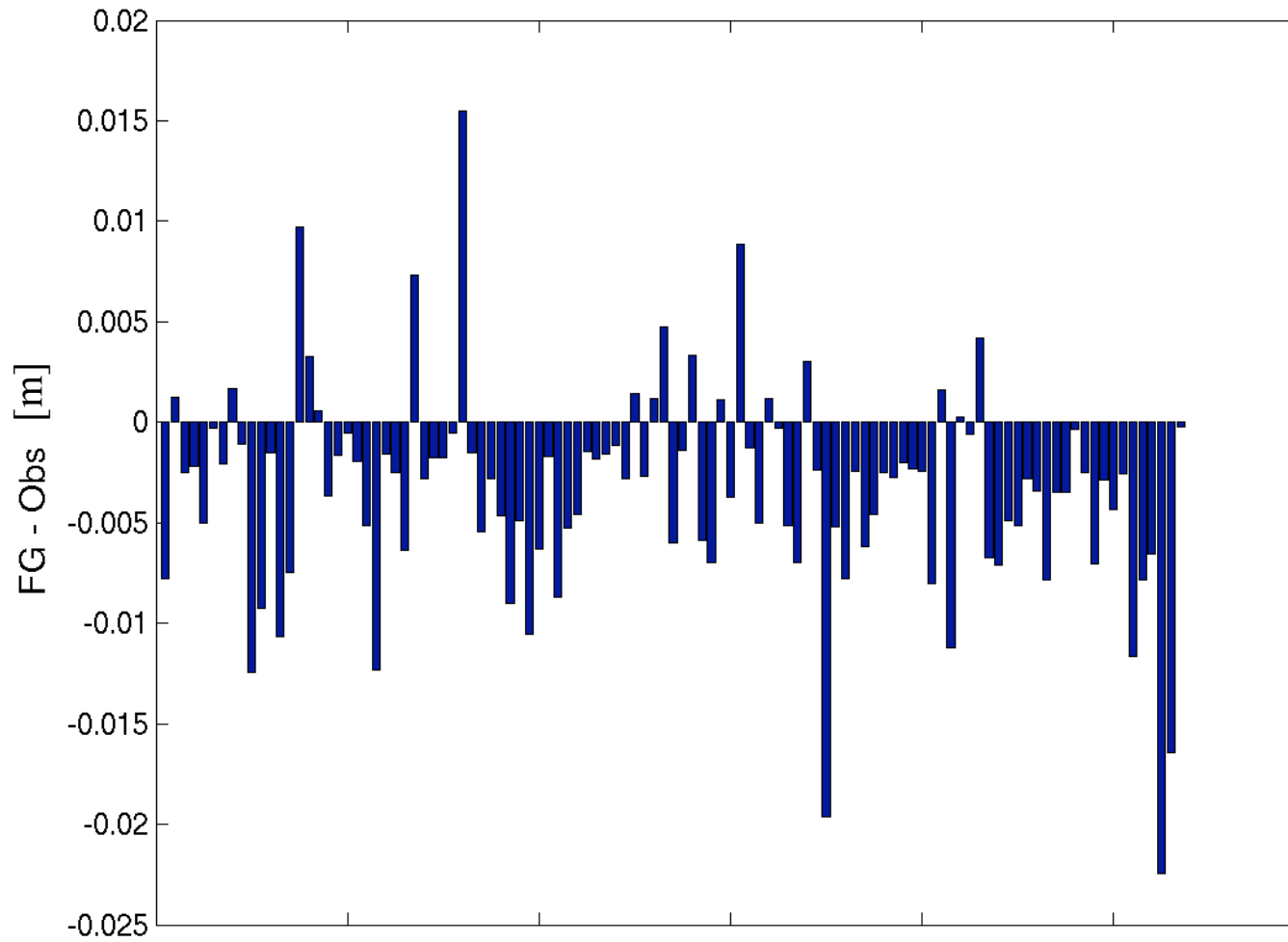
### Disadvantages:

- Only columnar water vapour
- There is be a bias and correlated errors



# First guess (6h forecast) – Observation

Average over 4 days





## *Bias correction*

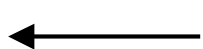
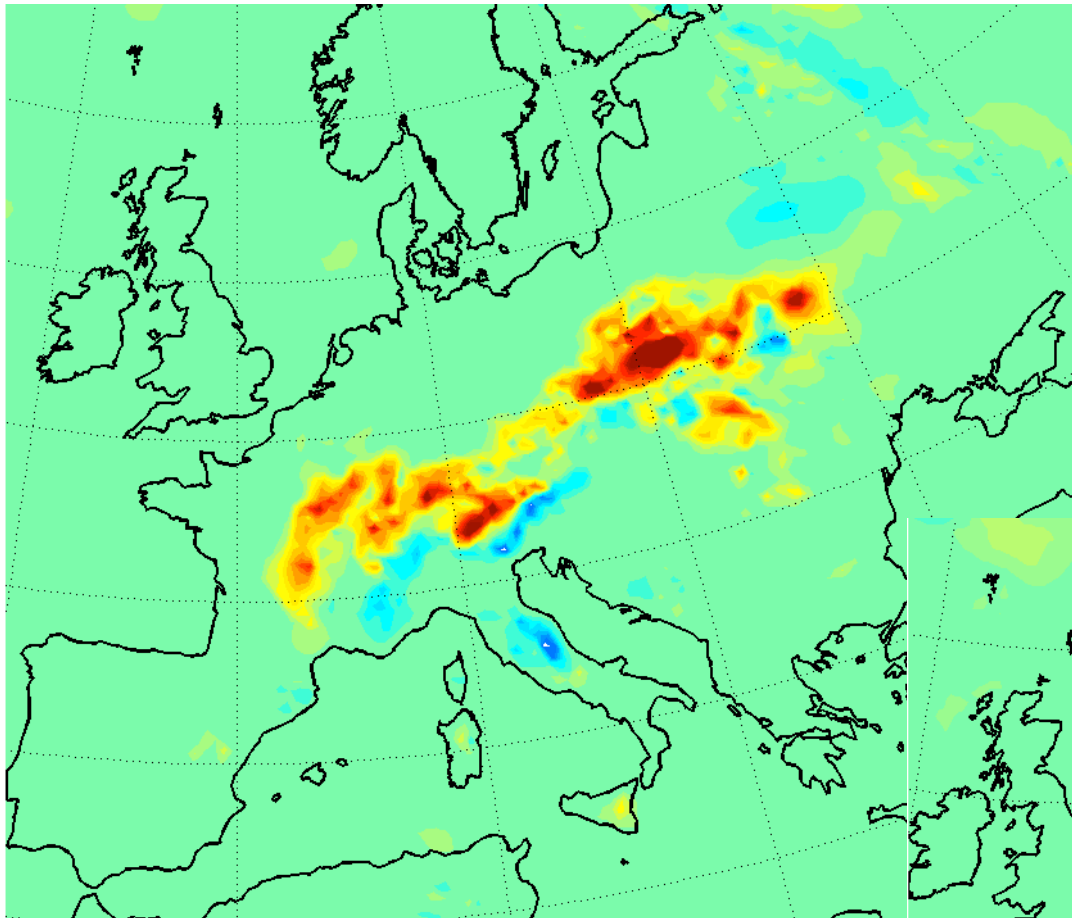
### What causes the bias?

- Different software
- Other differences in the processing, cut off angles...
- Antenna position and surroundings
- NWP model

Until we know it must be the modelled

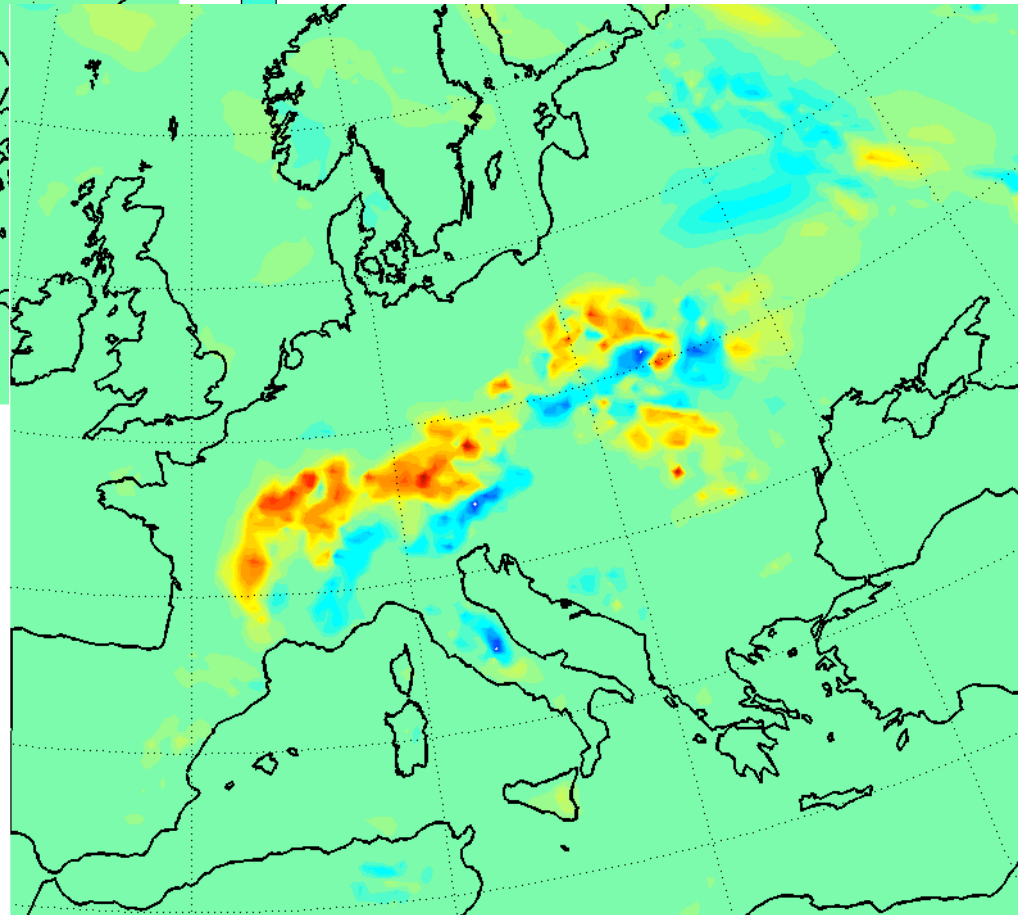
### Many different correction approaches

- Diurnal cycles
- Monthly means
- Slowly varying stochastic error
- ...



No bias correction

With bias correction



## *The observation operator - H*

Calculates a model equivalent of the observed quantity

- Transformation from spectral- to grid point space
- Vertical and horizontal interpolation to the observation point

In our case: A model ZTD at the station position

- ZHD from the ground pressure
- ZWD through integrated water vapour
- $ZTD = ZHD + ZWD$

The goal is to assimilate as raw data as possible

- Rinex data?

## *Error structures of the model – the B matrix*

Determines how an observation is spatially distributed

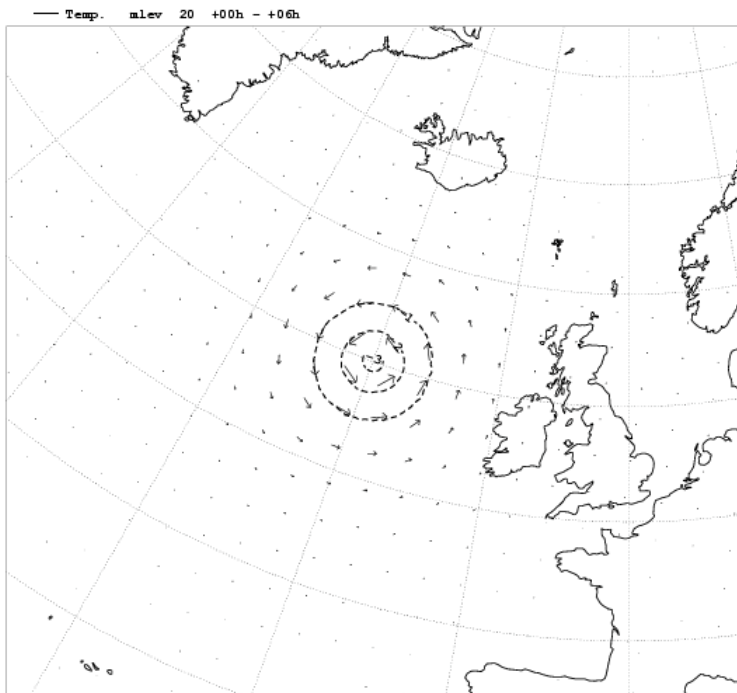
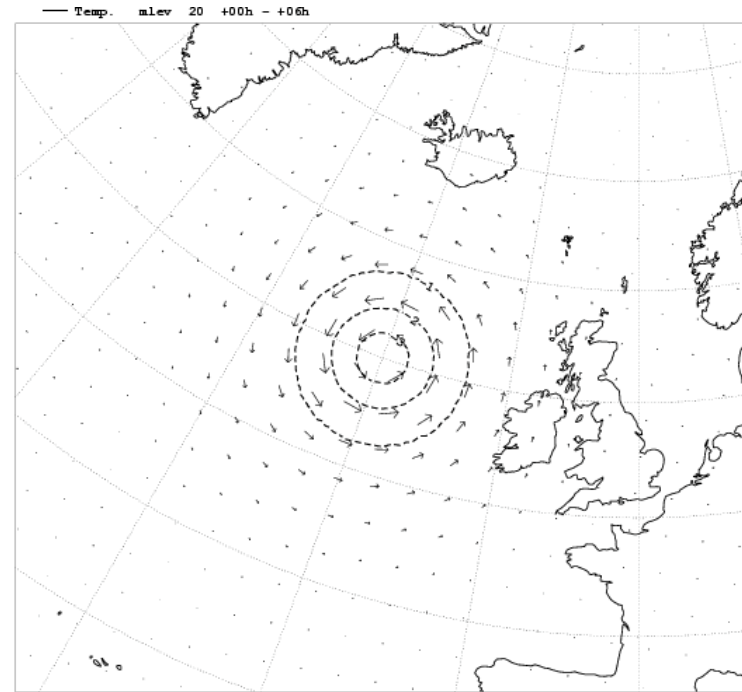
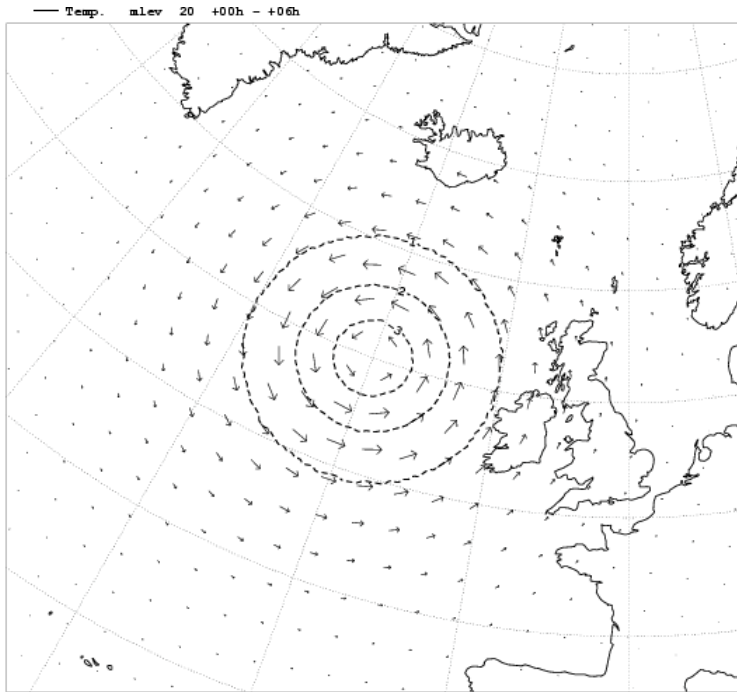
- Balance of the mass- and temperature fields
- Often assumed isotropic and homogeneous

The NMC-method

- 48-24 h forecast (valid at the same time)
- Originally a “temporary solution”
- Test with 36-18 h forecast
- Different resolutions (44, 33, 22 km)

Ensemble assimilation

- A number of 6 h forecasts with different initial conditions
- Observations are perturbed randomly
- Perturbed boundaries from a similar exp. at ECMWF
- Will resolve shorter length scales (to avoid representation errors)



Operational NMC method (44 km)

NMC method 22 km

Ensemble assimilation 22 km

## *Error struct. of the measurements – the R matrix*

The true ZTD error is not known

- Only “formal” errors from the processing
- Observation errors must be assumed or estimated

Correlated errors makes the matrix non-diagonal

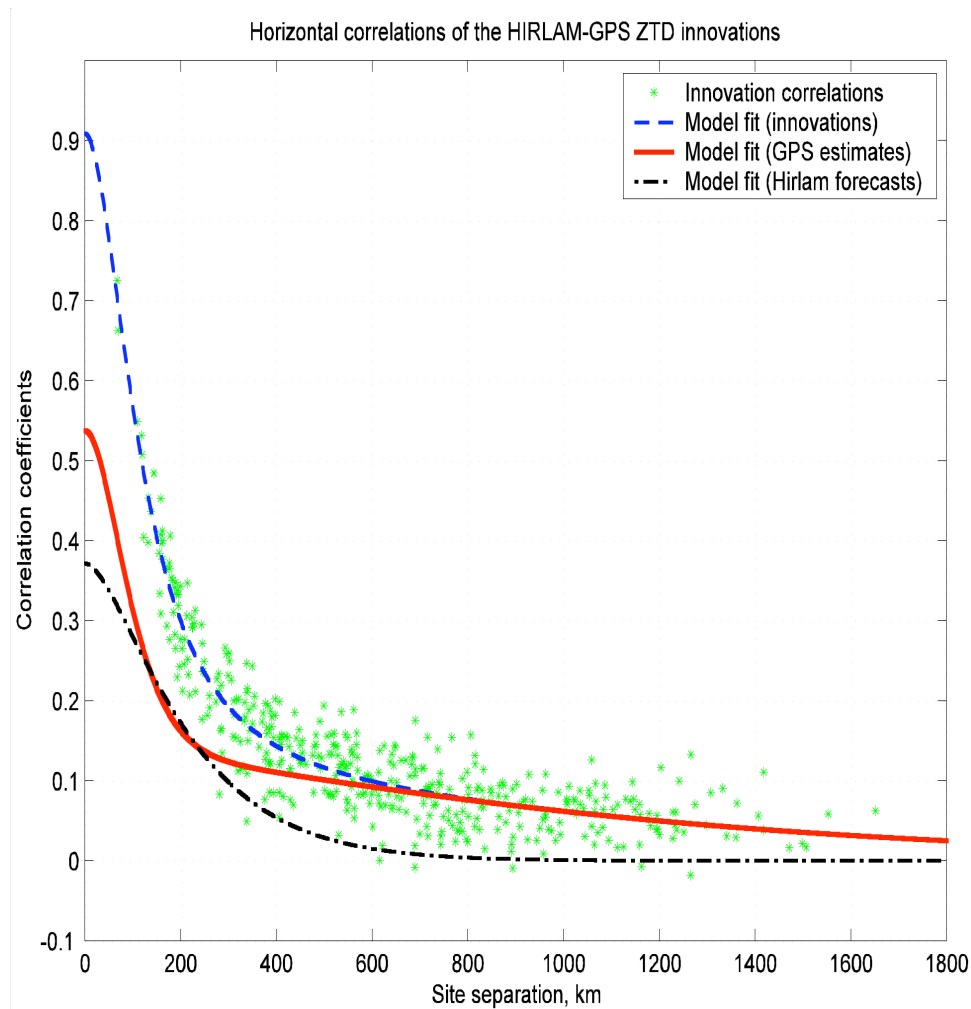
- Very costly to invert
- Needs to be rewritten and/or transformed

ZTD spatial error correlation model

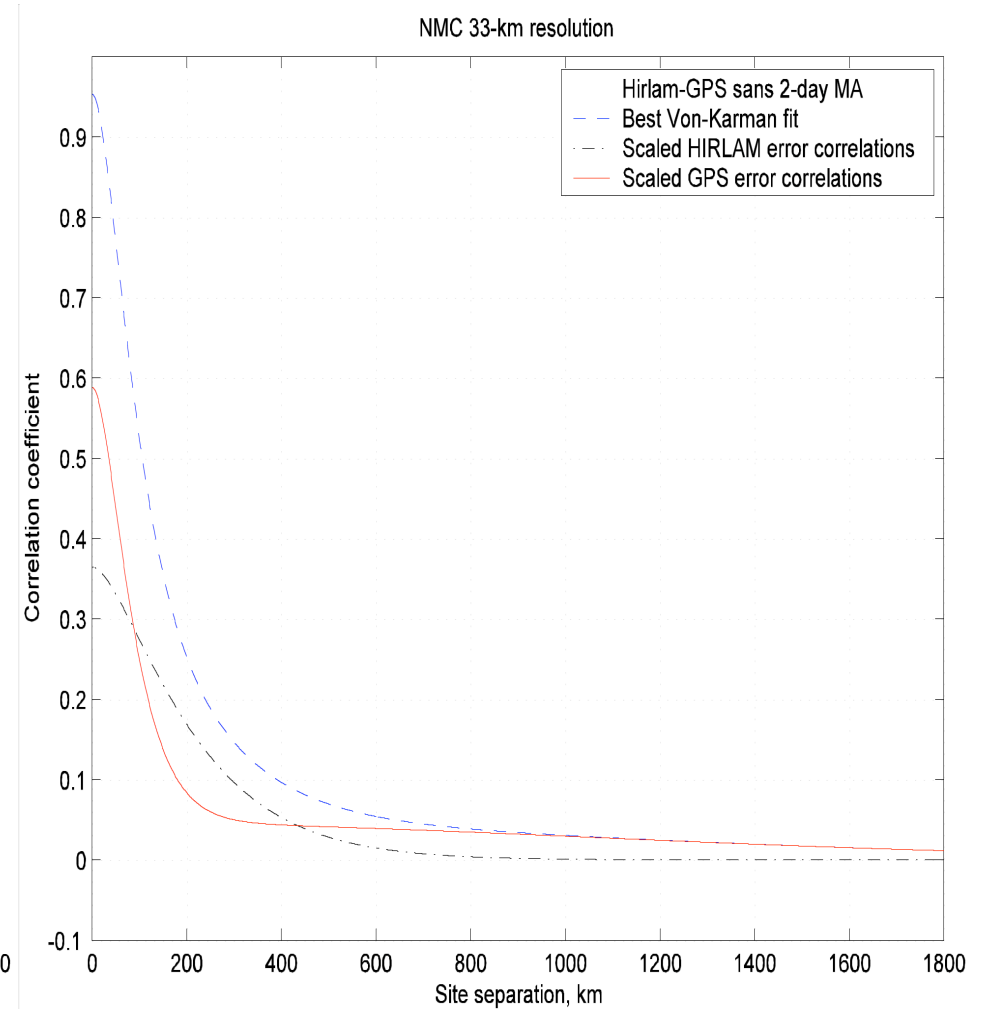
- Derived using other observations
- Derived from model – observation differences
- The effect of the bias correction

# Spatial correlation functions for ZTD (fg-obs) using the NMC-method (33 km)

## Uncorrected data



## Bias corrected data



## *The assimilation sequence*

The ZTD data is processed before entering the model

- E.g. hourly means
- A first quality control (or blacklist)

Preprocessing

- Data screening (quality control)
- Bias reduction

Observation operator

- Calculates ground pressure at the observation location
- Model profiles are adjusted to correct height
- A model ZTD is calculated

The minimisation

- Calculate residuals:  $Hx_b - y$
- Variational quality control
- Various transforms and normalisations
- The adjoint calculations is applied to get the model state variables



# Summary

## Moisture is a difficult quantity to assimilate

- Historically very few observations
- Large variation

## The bias problem

- What is the cause of the bias?
- How can we eliminate it as early as possible?

## Observation operator

- We want to assimilate as raw data as possible
- Process the ZTD data in the obs. operator?

## Error structures

- Model structure functions
- Observation error correlations